

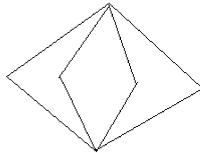


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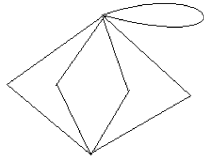
**Exercise 6.14:** For a 1D complex in 3D space we have that  $\beta_1$  is the number of tunnels (see page 225). Furthermore, from graph theory we also know that for a connected graph  $G = [V, E]$ , the cardinality of the cycle base of  $G$  is equal to  $\alpha_1 - \alpha_0 + 1$ .

Case (1): The set is homotopic to the 1D geometric (or Euclidean) complex shown in the following figure:



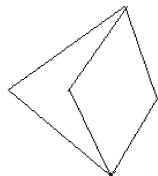
In this case we have  $8 - 6 + 1 = 3$  tunnels.

Case (2): The set is homotopic to the 1D geometric (or Euclidean) complex shown in the following figure:



In this case we have  $9 - 6 + 1 = 4$  tunnels.

Case (3): The set is homotopic to the 1D geometric (or Euclidean) complex shown in the following figure:



In this case we have  $6 - 5 + 1 = 2$  tunnels.